

Write the Given exponential equation as a logarithmic equation

1. $4^2 = 16$

$\log_4 16 = 2$

2. $e^{17} = a$

$\ln a = 17$

3. $10^4 = 10,000$

$\log 10,000 = 4$

4. $b^p = a$

$\log_b a = p$

Write the Given logarithmic equation as an exponential equation

5. $\log_7 x = 10$

$7^{10} = x$

6. $\ln x = 32$

$e^{32} = x$

7. $\log 1000 = 3$

$10^3 = 1000$

8. $\log_{\Delta} \Phi = \Psi$

$\Delta^{\Psi} = \Phi$

9. if $f(x) = \log_5 x$, find $f(125)$, $f\left(\frac{1}{25}\right)$, $f(\sqrt{5})$

$y = \log_5 125$

$5^y = 125$

$y = 3$

$y = \log_5 \frac{1}{25}$

$5^y = \frac{1}{25}$

$y = -2$

$y = \log_5 \sqrt{5}$

$5^x = \sqrt{5}$

$5^x = 5^{1/2}$

$x = \frac{1}{2}$

10. The loudness L , measured in decibels, of a sound of intensity x , measured in watts per square meter is $L(x) = 10 \log \frac{x}{10^{-12}}$. A Jet has an intensity level of 100 watts per square meter. How many decibels is a Jet?

$L(x) = 10 \log \frac{100}{10^{-12}}$
 $= 140$

140 decibels

Evaluate the following:

11. $\log_4 1$

$4^x = 1$

$x = 0$

12. $\ln e$

1

13. $\log_5 5$

$5^x = 5$

$x = 1$

14. ~~$7^{\log_7 12}$~~

12

15. ~~$\log_{12} 12^{15}$~~

15

16. ~~$\ln e^{32}$~~

32

17. ~~$10^{\log 14}$~~

14

17. $\log_5 \sqrt{5}$

$5^x = \sqrt{5}$

$x = \frac{1}{2}$

Write each as a single logarithm. Assume that all variables are positive.

$$18. 3\log_4 2 + \log_4 6$$

$$= \log_4 8 + \log_4 6$$

$$= \boxed{\log_4 48}$$

$$19. \frac{1}{3}\log_7 y - 6\log_7 z$$

$$= \log_7 y^{1/3} - \log_7 z^6$$

$$= \boxed{\log_7 \frac{\sqrt[3]{y}}{z^6}}$$

$$20. 3\log_2 x + \frac{1}{2}\log_2 y - 2\log(xz)$$

$$= \log_2 x^3 + \log_2 \sqrt{y} - \log(xz)^2$$

$$= \boxed{\log_2 x^3 \sqrt{y} - \log(xz)^2}$$

Use the properties of logarithms to expand the following. Express all exponents as coefficients.

$$21. \log_3 x^2 y^4$$

$$= \log_3 x^2 + \log_3 y^4$$

$$= \boxed{2\log_3 x + 4\log_3 y}$$

$$22. \log_{12} \frac{\sqrt{x}}{y^2}$$

$$= \log_{12} \sqrt{x} - \log_{12} y^2$$

$$= \boxed{\frac{1}{2}\log_{12} x - 2\log_{12} y}$$

$$23. \log_4 \frac{x\sqrt{y}}{z^{12}w^2}$$

$$= \log_4 x\sqrt{y} - \log_4 z^{12}w^2$$

$$= \log_4 x + \log_4 \sqrt{y} - \log_4 z^{12} + \log_4 w^2$$

$$= \boxed{\log_4 x + \frac{1}{2}\log_4 y - 12\log_4 z + 2\log_4 w}$$

Use the Change-of-Base to write the following in only natural logarithms. Then use your calculator to evaluate each.

$$24. \log_5 3$$

$$\frac{\ln 3}{\ln 5} \approx 0.6826$$

$$25. \log_{12} 13$$

$$\frac{\ln 13}{\ln 12} \approx 1.032$$

$$26. \log 80000$$

$$\frac{\ln 80000}{\ln 10} \approx 4.903$$

Solve the following. Round your answer to the nearest hundredth. Check for extraneous solutions.

$$27. 4^{2x+10} + 6 = 262$$

$$\log 4^{2x+10} = \log 256$$

$$2x+10 \log 4 = \log 256$$

$$\frac{\log 256 - 10 \log 4}{\log 4} = x$$

$$\boxed{x = -3}$$

$$28. 7e^{\frac{x}{4}} = 500$$

$$\frac{\ln 7e^{\frac{x}{4}}}{\ln 7} = \frac{\ln 500}{\ln 7}$$

$$4 \cdot \frac{x}{4} = \ln \frac{500}{7} \cdot 4$$

$$\boxed{x = 17.07}$$

$$29. \log_2 x - \log_2 3 = 4$$

$$\log_2 \frac{x}{3} = 4$$

$$2^4 = \frac{x}{3}$$

$$3 \cdot 16 = \frac{x}{3}$$

$$\boxed{x = 48}$$

$$30. \ln(x+2) + \ln(x+3) = \ln 30$$

$$\ln(x+2)(x+3) = \ln 30$$

$$(x+2)(x+3) = 30$$

$$x^2 + 5x + 6 = 30$$

$$x^2 + 5x - 24 = 0$$

$$(x-3)(x+8) = 0$$

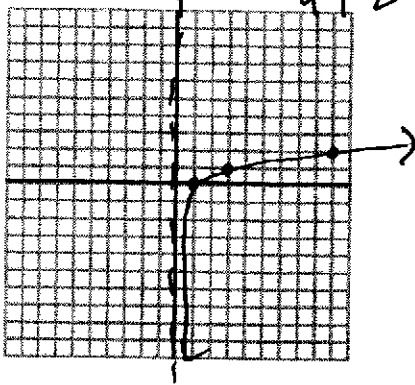
$$x = 3, -8$$

$$\boxed{x = 3}$$

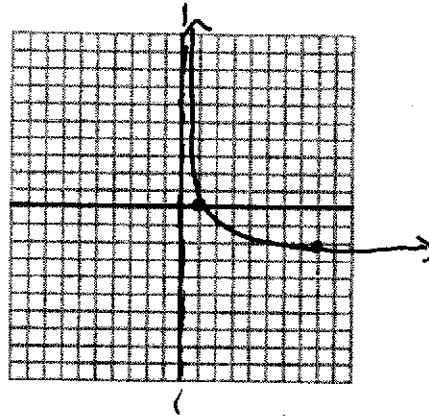
Graph the Following label at least 2 points:

31. $f(x) = \log_3 x$

X	Y
1	0
3	1
9	2

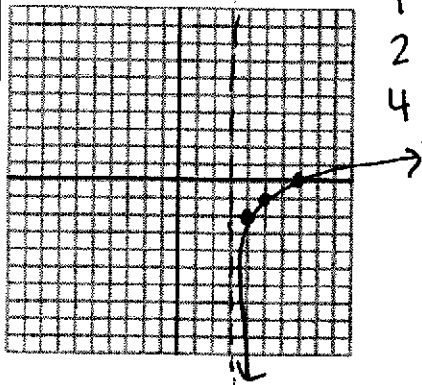


32. $f(x) = -\ln x$

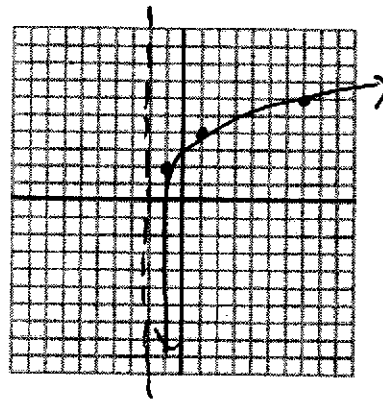


33. $f(x) = \log_2(x-3) - 2$

X	Y
1	0
2	1
4	2



34. $f(x) = 2\log_3(x+2) + 2$



X	Y
1	$0 \cdot 2 = 0$
3	$1 \cdot 2 = 2$
9	$2 \cdot 2 = 4$

35. The pH of ~~orange juice~~ ^{seawater} is 3.2, and the pH of milk is 6.1.

$$pH = -\log[H^+]$$

A. What are the hydrogen-ion concentrations of seawater and milk of magnesia?

seawater: $3.2 = -\log[H^+]$
 $10^{-3.2} = [H^+]$

Milk: $6.1 = -\log[H^+]$
 $10^{-6.1} = [H^+]$

B. How many times greater is the hydrogen-ion concentration of the seawater than that of milk of magnesia?

$$\frac{[H^+]_{\text{seawater}}}{[H^+]_{\text{milk}}} = \frac{10^{-3.2}}{10^{-6.1}} = 10^{2.9} \text{ times greater}$$

36. If Bob invests \$5,000 with a 4% interest rate compounded monthly, how long will it take until his investment has grown to \$7,000?

$$7000 = 5000 \left(1 + \frac{0.04}{12}\right)^{12t}$$

$$\frac{7}{5} = (1.00333)^{12t}$$

$$\ln \frac{7}{5} = \ln 1.00333^{12t}$$

$$\ln \frac{7}{5} = 12t \ln 1.00333$$

$$t \approx 0.43 \text{ yrs}$$

37. Find the amount accumulated from an investment of \$2,000 over 15 years at an interest rate of 6.2% compounded continuously.

$$A(t) = 2000 e^{0.062(15)}$$

$$= \$5069.02$$