

## Day 4 Elimination Using Multiplication

(# in front of variable)

Sometimes our coefficients are not the same and we have to multiply to create opposites before we can use elimination.

**Step 1:** Write the equations so variables are lined up.

**Step 2:** Multiply one or both of the equations by a number to obtain coefficients that are opposites for one of the variables.

**Step 3:** Add the equations to eliminate one of the variables.

**Step 4:** Solve the equation for the remaining variable.

**Step 5:** Substitute the value obtained in Step 4 into either one of the original equations and solve for the other variable.

**Step 6:** Write the solution as an ordered pair.  
(x, y)

## Example 1

$$\begin{array}{r}
 \bullet 5x + 6y = -8 \\
 \bullet 2x + 3y = -5 \cdot 2 \\
 \hline
 \bullet 4x + 6y = -10 \quad - \quad 4x + 6y = +10 \\
 \hline
 \phantom{4x + 6y = -10} \quad \quad \quad x = 2
 \end{array}$$

$$\begin{array}{r}
 5(2) + 6y = -8 \\
 10 + 6y = -8 \\
 -10 \quad -10 \\
 \hline
 6y = -18 \\
 6 \quad 6 \\
 \hline
 y = -3
 \end{array}$$

(x, y)  
(2, -3)

## Example 2

$$\begin{array}{r}
 6x - 2y = 10 \\
 3x - 7y = -19 \cdot 2 \\
 \hline
 \bullet 6x - 2y = 10 \\
 - \bullet 6x + 14y = +38 \\
 \hline
 \phantom{6x - 2y = 10} \quad \quad \quad 12y = 48 \\
 \phantom{6x - 2y = 10} \quad \quad \quad \frac{12}{12} \quad \frac{48}{12} \\
 \phantom{6x - 2y = 10} \quad \quad \quad y = 4
 \end{array}$$

$$\begin{array}{r}
 6x - 2(4) = 10 \\
 6x - 8 = 10 \\
 +8 \quad +8 \\
 \hline
 6x = 18 \\
 6 \quad 6 \\
 \hline
 x = 3
 \end{array}$$

(3, 4)

Solve the system

$$2x + 7y = 1$$

$$x + 5y = 2$$

Sometimes we will have to multiply both equations by a different number in order to have like terms.

**Example 3**

by

$$\begin{array}{r} 4x + 2y = 8 \\ 3x + 3y = 9 \end{array}$$

eliminate

$$\begin{array}{r} 12x + 6y = 12 \\ 6x + 6y = 18 \end{array}$$

$$\begin{array}{r} 6(1) + 6y = 18 \\ (1, 2) \quad -6 + 6y = 18 \\ \quad \quad \quad \frac{6y}{6} = \frac{24}{6} \\ \quad \quad \quad y = 2 \end{array}$$

$$\begin{array}{r} 6x = 6 \\ x = 1 \end{array}$$

**Example 4**

$$\begin{aligned}5x - 3y &= 6 \\ 2x + 5y &= -10\end{aligned}$$

**Example 5** A buffet has one price for adults and another price for children. The Taylor family has 2 adults and 3 children and their bill was \$40.50. The Wong family has 3 adults and 1 child and their bill was \$38. What is the price for adults and children at the buffet?

