

Factoring

I can factor the greatest common factor out of an expression.

I can factor an expression by grouping.

I can factor quadratic expressions in standard form.

Find the greatest common factor (GCF) of the terms

$$4x, 12$$

$$4$$

$$\underline{6}x^3, \underline{12}x^2, \underline{15}x$$

$$3x$$

$$4x^3y^4, 8x^2y^3, 12xy^2$$

$$4xy^2$$

Factor out the GCF

$$\underbrace{4a^2b^2}_{2ab^2} - \underbrace{10ab^3}_{2ab^2} + \underbrace{18a^3b^4}_{2ab^2}$$

$$2ab^2(2a - 5b + 9a^2b^2)$$

Factor out the GCF

$$-2b^3 + 10b^2 + 8b$$

$$2b(-b^2 + 5b + 4) \quad -2b(b^2 - 5b - 4)$$

You Try

Factor out the GCF

$$\frac{-5y^2}{-5y} + \frac{10y}{-5y}$$

$$-5y(y - 2)$$

Factor out the Greatest Common Binomial Factor

$$4x(x-3) + 5(x-3)$$

$$(x-3)(4x+5)$$

You Try

Factor out the Greatest Common Binomial Factor

$$4a(a-3) + 3(a-3)$$

$$(a-3)(4a+3)$$

Factor by grouping

$$4x - 4y + ax - ay$$

$$4(x-y) + a(x-y)$$

$$(x-y)(4+a)$$

Factor by grouping

$$6x^2 + 9x - 10x - 15$$

$$3x(2x+3) - 5(2x+3)$$

$$(2x+3)(3x-5)$$

Factor COMPLETELY by grouping

$$6x^2 + 8x + 18x + 24$$

$$2(3x^2 + 4x + 9x + 12)$$

$$2[x(3x+4) + 3(3x+4)]$$

$$2(x+3)(3x+4)$$

You Try (make sure they do this one)

Factor by grouping

$$2x^2 + 2x + x + 1$$

$$2x(x+1) + 1(x+1)$$

$$(x+1)(2x+1)$$

How to Factor a Quadratic

Factoring quadratics in the form $ax^2 + bx + c$

1. Factor out the GCF
2. Multiply a and c
3. Find two factors of ac that add to b
 - *If ac is negative, factors must have opposite signs
 - *If ac is positive, factors must have same (+ or -) signs
4. Re-write equation with b split up into factors
5. Find the GCF by grouping
6. Factor the GCF of the whole

(X) \Rightarrow when $a=1$
 Factor each quadratic expression

$2a^2 + 9a + 4$ $\begin{matrix} 8 \\ 1 & 8 \\ 2 & 4 \end{matrix}$ $x^2 - 6x - 7$ $\begin{matrix} -7 \\ +1 & -7 \end{matrix}$

$2a^2 + a + 8a + 4$ Factor $(x+1)(x-7)$

$a(2a+1) + 4(2a+1)$ Solve: $x+1=0$ $x-7=0$

$x=-1$ $x=7$

$(2a+1)(a+4)$

YOUR TURN!

Factor each quadratic expression

$x^2 + 6x + 8$

$(x+4)(x+2)$

$x^2 - 10x + 16$

$(x-2)(x-8)$

Factor each quadratic expression

$$56 + 10x - x^2$$

$$35 - 12x + x^2$$

$$\begin{aligned}
 & -x^2 + 10x + 56 \quad +4 \quad -14 \\
 & -1(x^2 - 10x - 56) \\
 & -(x+4)(x-14)
 \end{aligned}$$

YOUR TURN!

Factor each quadratic expression

~~2x^2 + 13x + 5~~

$$\begin{array}{ccc}
 2x^2 & +13x & +5 \\
 \downarrow & \swarrow \searrow & \downarrow \\
 2x^2 & +3x & +10x & +5
 \end{array}$$

$$2x^2 + 3x + 10x + 5$$

$$x(2x+3) + 5(2x+3)$$

$$(2x+3)(x+5)$$

$$\begin{array}{ccc}
 & 30 & \\
 1 & 30 & \\
 2 & 15 & \\
 3 & 10 & \\
 5 & 6 &
 \end{array}$$

$$4x^2 - 13x + 3$$

$$\begin{aligned}
 & 4x^2 - 12x - x + 3 \\
 & 4x(x-3) - 1(x-3) \\
 & (4x-1)(x-3)
 \end{aligned}$$