

$$(a+b)^n \leftarrow n$$

n decrease
 0 increase

$$| a^4 \cancel{b^1} + 4a^3 b^1 + 6a^2 b^2 + 4a^1 b^3 + \cancel{b^4} |$$

$$a^4 + 4a^3 b + 6a^2 b^2 + 4ab^3 + b^4$$

1 4 6 4 1 3. $(x-5)^4$ $a=x$ $b=-5$ $n=4$

$$1(x)^4(-5)^0 + 4(x)^3(-5)^1 + 6(x)^2(-5)^2$$

$$+ 4(x)^1(-5)^3 + 1(x)^0(-5)^4$$

$$1(x^4)(1) + 4(x^3)(-5) + 6(x^2)(25)$$

$$+ 4(x)(-125) + 1(1)(625)$$

$$x^4 - 20x^3 + 150x^2 - 500x + 625$$

$$1 \quad \cancel{5} \quad 10 \quad 10 \quad \cancel{5} \quad 1 \quad 4. \quad (3x+4)^5 \quad a=3x \quad b=4 \quad n=5$$

$$1(3x)^5(4)^0 + 5(3x)^4(4)^1 + 10(3x)^3(4)^2 + 10(3x)^2(4)^3 + 5(3x)^1(4)^4 + 1(3x)^0(4)^5$$

$$1(\underline{243}x^5)(\underline{1}) + 5(\underline{81}x^4)(\underline{4}) + 10(\underline{27}x^3)(\underline{16}) + 10(\underline{9}x^2)(\underline{64}) + 5(\underline{3}x)(\underline{256}) + 1(\underline{1})(\underline{1024})$$

$$243x^5 + 1620x^4 + 4320x^3 + 5706x^2 + 3840x + 1024$$

$$1 \quad 6 \quad 15 \quad 20 \quad 15 \quad 6 \quad 1 \quad 8. \quad (4x+3y)^6 \quad a=4x \quad b=3y \quad n=6$$

$$1(4x)^6(3y)^0 + 6(4x)^5(3y)^1 + 15(4x)^4(3y)^2 + 20(4x)^3(3y)^3 + 15(4x)^2(3y)^4 + 6(4x)^1(3y)^5 + 1(3x)^0(3y)^6$$

$$15(\underline{16}x^2)(\underline{81}y^4)$$

$$19440x^2y^4$$

$$(3x)^5 = 3x \cdot 3x \cdot 3x \cdot 3x \cdot 3x$$
$$3^5 x^5$$

2-3 Factoring Polynomials

(Book 6.4 pg. 353-)

Objectives:

- I can factor a polynomial by GCF, special factoring, and factor by grouping
- I can find multiple representations of factored polynomials

$a = 1 \rightarrow$ short cut
Factor the following:

$x^2 - 7x + 10$ $1 \cdot 10 = 10$ $2x^2 - 3x - 2$ $2 \cdot 2 = -4$

$(x-2)(x-5)$ $(-2, -5)$ $(2, 2)$ $(+1, -4)$

$x^2 - 2x - 5x + 10$ $2x^2 + x - 4x - 2$

$x(x-2) - 5(x-2)$ $x(2x+1) - 2(2x+1)$

$(x-2)(x-5)$ $(2x+1)(x-2)$

Greatest Common Factors pg. 355-356

(A) $6x^3 + 15x^2 + 6x$

$6x^3 + 15x^2 + 6x$

Write out the polynomial.

$x(6x^2 + 15x + 6)$

Factor out a common monomial, an x .

$3x(2x^2 + 5x + 2)$

Factor out a common monomial, a 3.

$3x(2x+1)(x+2)$

Factor into simplest terms.

Note: The second and third steps can be combined into one step by factoring out the greatest common monomial.

(B) $2x^3 - 20x$

$2x^3 - 20x$

Write out the polynomial.

$2x(x^2 - 10)$

Factor out the greatest common monomial.

$x^2 + 0x - 10$

$1(-10) = -10$

$$3x(2x^2 + 5x + 2)$$

$$3x[2x^2 + x + 4x + 2]$$

$$3x[x(2x+1) + 2(x+1)]$$

$$3x(2x+1)(x+1)$$

$$2 \cdot 2 = 4$$

1	4
2	2

Factor.

$$3x^3 + 7x^2 + 4x$$

$$x(3x^2 + 7x + 4)$$

$$x[3x^2 + 3x + 4x + 4]$$

$$x[3x(x+1) + 4(x+1)]$$

$$x[(x+1)3x + 4]$$

$$x(x+1)(3x+4)$$

$$12a^4b + 8a^3b^3 - 10a^2b^4$$

$$\frac{1}{2} \cdot 2$$

$$\frac{2}{2} \cdot 6$$

$$\frac{3}{3} \cdot 4$$

$$6x^2 + 3x + 9$$

$$3[2x^2 + x + 3]$$

$$2 \cdot 6 = 6$$

$$\begin{array}{r} 1 \quad 6 \\ -2 \quad +3 \\ \hline -4 \end{array}$$

Special Factoring Patterns pg. 355

Remember the factoring patterns you already know:

Difference of two squares: $a^2 - b^2 = (a - b)(a + b)$

Perfect square trinomials: $a^2 + 2ab + b^2 = (a + b)^2$

$$a^2 - 2ab + b^2 = (a - b)^2$$

There are two other factoring patterns that will prove useful:

Sum of two cubes: $a^3 + b^3 = (a + b)(a^2 - ab + b^2)$

Difference of two cubes: $a^3 - b^3 = (a - b)(a^2 + ab + b^2)$

$$a =$$

$$b =$$

Factor. $(3x)^2$

$\sqrt[3]{x^3} = 27$
 $a = x \quad b = 3$
 $(x-3)(x^2 + 3x + 9)$

$27x^3 + 64$
 $a = 3x \quad b = 4$
 $(3x+4)(9x^2 - 12x + 16)$

$8x^3 + 64$
 $8(x^3 + 8)$
 $a = x \quad b = 2$
 $8(x+2)(x^2 - 2x + 4)$

$x^3 + 4$
 $a = x \quad b =$
irreducible

$4x^2 - 36$

Factoring by Grouping pg. 357

A $x^3 + x^2 + x + 1$

Write out the polynomial.

$$x^3 - x^2 + x - 1$$

Group by common factor.

$$(x^3 - x^2) + (x - 1)$$

Factor.

$$x^2(x - 1) + 1(x - 1)$$

Regroup.

$$(x^2 + 1)(x - 1)$$

B $x^4 + x^3 + x + 1$

Write out the polynomial.

$$x^4 + x^3 + x + 1$$

Group by common factor.

$$(\underline{\quad} + \underline{\quad}) + (x + 1)$$

Factor.

$$\underline{\quad}(x + 1) + \underline{\quad}(x + 1)$$

Regroup.

$$(\underline{\quad} + \underline{\quad})(x + 1)$$

Apply sum of two cubes to the first term.

$$(\underline{\quad} - \underline{\quad} + 1)(x + 1)(x + 1)$$

Substitute this into the expression and simplify.

$$(\underline{\quad})^2(\underline{\quad} - \underline{\quad} + 1)$$

Factor by Grouping.

$$x^3 + 3x^2 + 3x + 2$$

$$x^3 - 3x^2 + x - 3$$