$a = 0.3$

$r = \frac{1}{10}$

$n = ?\ 5$

$$\frac{.000003}{0.3} = \frac{0.3\left(\frac{1}{10}\right)^n}{0.3}$$

$$.00001 = \left(\frac{1}{10}\right)^n$$

$$\left(\frac{1}{10}\right) \quad - \left(\frac{1}{10}\right)$$

$a = 5000$

$r = 1.04$

5000 $\quad +4\%$

$n = 9$

$.04\% \quad \frac{4}{100}$

7-3 Exponential Review

I can apply exponential properties and use them

I can model real-world situations using exponential functions

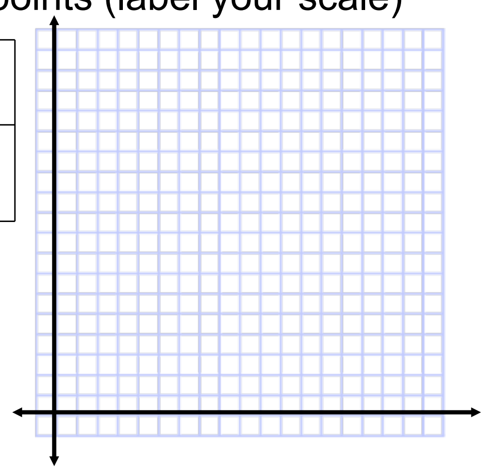
Warm-Up

1. Find the next three terms in the sequence

   2, 6, 18, 54, ____ , ____ , ____
   ·3

2. Fill in the table, then plot the points (label your scale)

n	0	1	2	3	4	5
f(n)	1	2	4	8	16	



If we connected the points, what do you notice about the graph?

Have you ever seen a graph like this before?

EXPONENTIAL FUNCTION

$$f(x) = a(b)^x \leftarrow \text{Exponent}$$

time

$x=0$

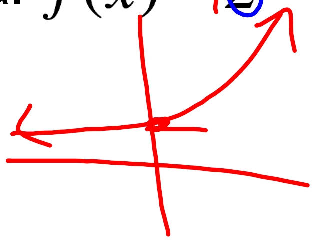
Initial Value (y-intercept)

Base (Multiplier) rate

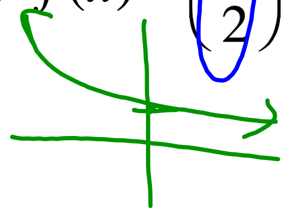
$f(n) = a \cdot r^n$

Graph the following functions on a calculator and sketch.
Be sure to plot the y-intercept

a. $f(x) = 2^x$



b. $f(x) = \left(\frac{1}{2}\right)^x$



What did you notice about the graphs and their equations?

$f(x) = a(b)^x$

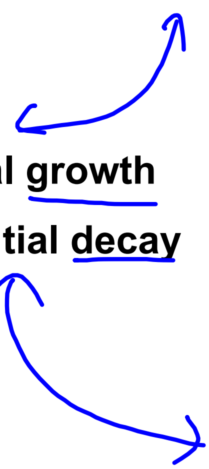
<u>Exponential Growth and Decay</u>

When b>1, the function represents **exponential growth**

When 0<b<1, the function represents **exponential decay**

$f(x) = 2\left(\frac{7}{3}\right)^x$

growth



Determine whether each function represents growth or decay

a. $f(x) = 13\left(\frac{1}{3}\right)^x$ b. $g(x) = \left(\frac{3}{2}\right)^x$

D G

Write one equation that represents growth and one that represent decay

growth

$f(x) = 2\left(\frac{4}{2}\right)^x$

decay

$f(x) = 69\left(\frac{1}{2}\right)^x$

growth/decay

$$f(t) = a(1 \pm r)^t$$

growth → time

initial decay rate

DECIMAL

~~3~~% $.03$

~~.~~25% $.0025$

John researches a baseball card and find that it is currently worth $3.25. However, it is supposed to increase in value 11% per year. pg 686 $f(t) = a(1 \pm r)^t$

a) Write an exponential equation to represent this situation

$f(t) = 3.25(1+.11)^t$

b) How much will the card be worth in 10 years?

$= 3.25(1+.11)^{10} = \$9.23$

c) Use your graphing calculator to determine in how many years will the card be worth $26.

x → time

y → $

$y_1 = 3.25(1+.11)^x$

$y_2 = 26$

$\boxed{19.93 \text{ years}}$

You Try!

On federal income tax returns, self employed people can depreciate the value of business equipment. Suppose a computer valued at $2765 depreciates at a rate of 30% per year. pg 704 $f(t) = a(1 \pm r)^t$

a) Write an exponential equation to model this situation

$2765(1-.3)^t$

b) How much will this computer be worth in 5 years?

$464.71

c) Use your graphing calculator to determine in how many years will the computer be worth $350.

$y_1 = 2765(1-.3)^x$

$y_2 = 350$

intersect 5.79 yrs

The population of Orem in 1950 was 4,000 and was increasing at a rate of 2.6% per year.

a) Predict the population of Orem in 1975 and 2000.

$f(t) = 4000(1 + .026)^t$

$1975 \to f(25)$ 7599

$2000 \to f(50)$ 14,435

b) Using your graphing calculator, predict when Orem's population will hit 200,000 people.

152.41 yrs

$1950 + 152.41$

2102.41

The half-life of Carbon-14 is 5700 years. If a fossil decayed from 15 grams to 1.875 grams, how old is the fossil? (use your calculator)

Compound Interest Formula

$$A(t) = P\left(1 + \frac{r}{n}\right)^{nt}$$

P is the principal

r is the annual interest rate

n is the number of compounding periods per year

t is the time in years

Write an equation then find the final amount for each investment.

a. $1000 at 8% compounded semiannually for 15 years

$$A(t) = P\left(1 + \frac{r}{n}\right)^{nt}$$

You Try!

b. $1750 at 3.65% compounded daily for 10 years

Using a calculator, determine how many years it will take for the amount to reach $4000.

Investigate the growth of $1 investment that earns 100% annual interest (r=1) over 1 year as the number of compounding periods, n, increases.

Compounding schedule	n	$1\left(1+\frac{1}{n}\right)^n$	Value of A
annually	1		
semiannually	2		
quarterly	4		
monthly	12		
daily	365		
hourly	8760		
every minute	525600		

What does the value of A approach?

The value e is called the natural base

The exponential function with base e, $f(x)=e^x$, is called the natural exponential function.

$$e \approx 2.71828182827$$

what you need to know is $e \approx 2.7$

Evaluate $f(x) = e^x$ for

a. $x = 2$

b. $x = \frac{1}{2}$

c. $x = -1$

Many banks compound the interest on accounts daily or monthly. However, some banks compound interest continuously, or at every instant, by using the *continuous compounding formula.*

Continuous Compounding Formula

If P dollars are invested at an interest rate r, that is compounded continuously, then the amount, A, of the investment at time t is given by

$$A(t) = Pe^{rt}$$

A person invests \$1550 in an account that earns 4% annual interest compounded continuously.

a. Write an equation to represent this situation

b. Using a calculator, find when the value of the investment reaches \$2000.

Pg 730 $A(t) = Pe^{rt}$

An investment of \$1000 earns an annual interest rate of 7.6%.

Compare the final amounts after 8 years for interest *compounded quarterly* and for interest *compounded continuously.*

CHECK:

-What is the difference between growth and decay?

-What does each piece of the equation $y = a(b)^x$ represent?