

Unit 14 Review

Factor out the greatest common factor:

1. $4m^3 + 8m^2 - 16m$
 $4m(m^2 + 2m - 4)$

2. $x(x-4) + 6(x-4)$
 $(x-4)(x+6)$

Factor completely:

3. $w^2 + 13w + 40$
 $(w+8)(w+5)$

4. $2x^2 + 13x + 15$
 $\downarrow \quad \swarrow$
 $2x^2 + 3x + 10x + 15$
 $x(2x+3) + 5(2x+3)$
 $(2x+3)(x+5)$

5. $x^2 + 4x + 3$
 $(x+3)(x+1)$

Simplify: LCD: $2x$

$\frac{2 \cdot 7}{6^2 \cdot x} + \frac{5 \cdot x}{2 \cdot x} = \frac{14}{2x} + \frac{5x}{2x} = \frac{14+5x}{2x}$

7. $\frac{2x}{x-3} + \frac{x-3}{2x}$

$\frac{2x}{x-3} \cdot \frac{2x}{x-3} = \frac{4x^2}{(x-3)^2}$

Solve the equation for the variable:

8. $-18 + 13y + 3 = 3(5y - 1) - 2$
 $13y - 15 = 15y - 3 - 2$
 $13y - 15 = 15y - 5$
 $-13y + 5 \quad -13y + 5$
 $\frac{10}{2} = \frac{2y}{2}$
 $y = 5$

9. $8(w-2) = 32$
 $8w - 16 = 32$
 $+16 \quad +16$
 $\frac{8w}{8} = \frac{48}{8}$
 $w = 6$

10. $-\underline{x} + 3 + \underline{2x} = 18$

$x + 3 = 18$
 $-3 \quad -3$
 $x = 15$

11. $6y = 28 - 4$

$\frac{6y}{6} = \frac{24}{6}$
 $y = 4$

Find the LCD of the following:

12. $\frac{x+4}{x^2-4}$ and $\frac{-2x-2}{x^2-4}$

x^2-4

13. $\frac{4x+12}{x^2+5x+6}$ and $\frac{5x+15}{10x+20}$

$(x+2)(x+3)$ ~~$(x+2)$~~

LCD: $10(x+2)(x+3)$

Add, Subtract, Multiply, or Divide:

14. $\frac{x}{3x-6} \cdot \frac{x-2}{x+9} = \frac{x^2-2x}{(3x-6)(x+9)}$ OR $\frac{x(x-2)}{3(x-2)(x+9)}$

15. $\frac{x+3}{x^2+8x+15} \div \frac{x^2-25}{x-5} \rightarrow \frac{x+3}{x^2+8x+15} \cdot \frac{x-5}{x^2-25} = \frac{(x+3)}{(x+3)(x+5)} \cdot \frac{(x-5)}{(x+5)(x-5)}$
 $= \frac{(x+3)\cancel{(x-5)}}{(x+3)(x+5)(x+5)\cancel{(x-5)}} = \frac{1}{(x+5)^2}$

LCD: $x(1+x)$
16. $\frac{1}{1+x} + \frac{1-x}{x}$

$\frac{1(x)}{(1+x)(x)} + \frac{(1-x)(1+x)}{x(1+x)} = \frac{x + 1 - x^2}{x(1+x)}$ OR $\frac{-x^2+x+1}{x(1+x)}$

LCD: $(x+2)(x-2)$

17. $\frac{3}{x^2-4} - \frac{x+5}{x+2} \cdot \frac{x-2}{x-2} = \frac{3}{(x+2)(x-2)} - \frac{(x+5)(x-2)}{(x+2)(x-2)} = \frac{3 - (x^2+3x-10)}{(x+2)(x-2)}$
 $= \frac{-x^2-3x+13}{(x+2)(x-2)}$

16. **Art** A glassblower can produce several sets of simple glasses in about 3 hours. When the glassblower works with an apprentice, the job takes about 2 hours. How long would it take the apprentice to make the same number of sets of glasses when working alone?

* $\neq 0$
LCD: $6t$

$\frac{1 \cdot 6t}{3} + \frac{1 \cdot 6t}{t} = \frac{1 \cdot 6t}{2}$

$2t + 6 = 3t$
 $-2t \quad -2t$

$t = 6 \text{ hrs}$