

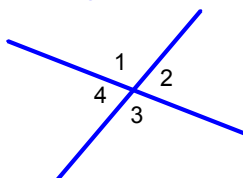
1. Supplementary Angles: 2 angles whose measures add to 180 degrees

2. Complementary Angles: 2 angles whose measures add to 90 degrees

3. Vertical Angles: 2 nonadjacent angles that are formed by two intersecting lines (they are congruent)

$\angle 1$ and $\angle 3$ are vertical angles

$\angle 2$ and $\angle 4$ are vertical angles



4. Transitive Property: If $a=b$ and $b=c$, then $a=c$ (a special type of substitution where you substitute a whole side)

5. Substitution Property: If $a + b = c$ and $a=d$, then $d + b = c$.

6. Reflexive Property: When you say something is equal or congruent to itself ($3 = 3$, $BC = BC$, $\angle 1 \cong \angle 1$)

7. Linear Pair: 2 angles that are adjacent and supplementary (form a line)



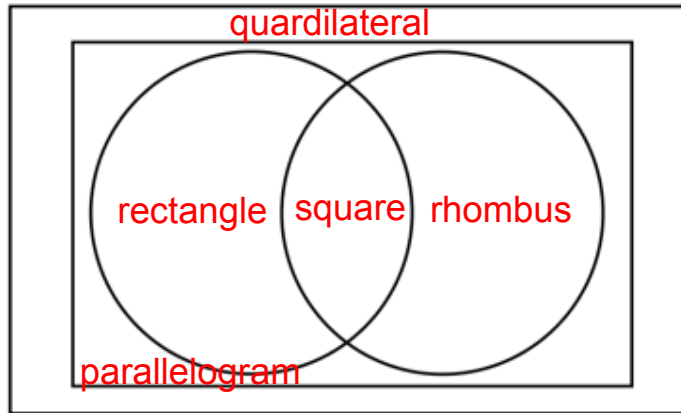
8. Subtraction Property: If $a=b$, then $a-c=b-c$ (you can subtract the same thing from both sides of an equation and it is still equal)

9. Addition Property: If $a=b$, then $a+c=b+c$ (you can add the same thing from both sides of an equation and it is still equal)

10. Adjacent Angles: 2 angles that share a common vertex and a common side (next to each other)



11.



Quadrilateral: A polygon with 4 sides (and 4 vertices)

Parallelogram: A quadrilateral with opposite sides parallel

Rectangle: A quadrilateral with all four angles congruent

Rhombus: A quadrilateral with all four sides congruent

Square: A quadrilateral with all four sides and all four angles congruent

Decide whether the statement is *sometimes*, *always*, or *never* true.

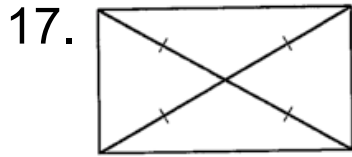
12. A rhombus is equilateral. **Always**

13. The diagonals of a rectangle are perpendicular. **Sometimes**

14. The opposite angles of a rhombus are supplementary.
Sometimes

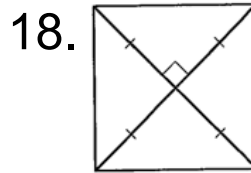
15. The diagonals of a rectangle bisect each other. **Always**

16. The consecutive angles of a square are supplementary
Always



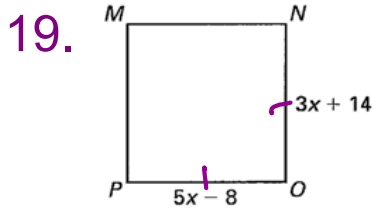
Rectangle

(Diagonals Congruent)

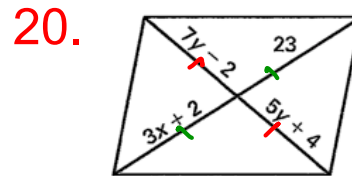


Square

(Diagonals congruent and diagonals are perpendicular)



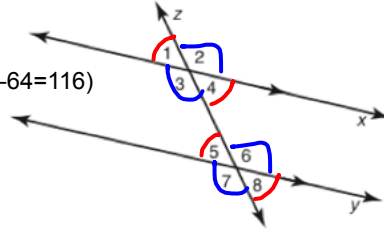
$$\begin{aligned}
 5x - 8 &= 3x + 14 \\
 -3x &\quad -3x \\
 \hline
 2x - 8 &= 14 \\
 +8 &\quad +8 \\
 \hline
 2x &= 22 \\
 \frac{2x}{2} &= \frac{22}{2} \\
 \boxed{x=11}
 \end{aligned}$$



$$\begin{aligned}
 7y - 2 &= 5y + 4 \\
 -5y &\quad -5y \\
 \hline
 2y - 2 &= 4 \\
 +2 &\quad +2 \\
 \hline
 2y &= 6 \\
 \frac{2y}{2} &= \frac{6}{2} \\
 \boxed{y=3}
 \end{aligned}$$

$$\begin{aligned}
 3x + 2 &= 23 \\
 -2 &\quad -2 \\
 \hline
 3x &= 21 \\
 \frac{3x}{3} &= \frac{21}{3} \\
 \boxed{x=7}
 \end{aligned}$$

21. $m\angle 1$: 64 deg (given)
 $m\angle 2$: 116 deg (linear pair with $\angle 1$, $180-64=116$)
 $m\angle 3$: 116 deg (vertical to $\angle 2$)
 $m\angle 4$: 64 deg (vertical to $\angle 1$)
 $m\angle 5$: 64 deg (corresponding to $\angle 1$)
 $m\angle 6$: 116 deg (corresponding to $\angle 2$)
 $m\angle 7$: 116 deg (vertical to $\angle 6$)
 $m\angle 8$: 64 deg (vertical to $\angle 7$)



Recall:

Vertical angles (angles opposite each other) are congruent

Corresponding angles (angles in the same place of each intersection) are congruent

Linear Pair (2 angles that form a straight line) are supplementary (add to 180 degrees)

22. In the figure above list a pair of angles for the following terms:

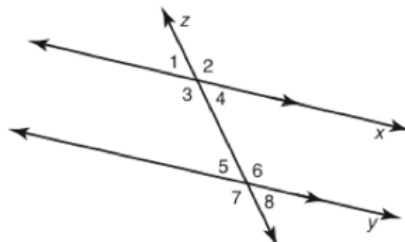
Alternate interior angles: $\angle 3$ & $\angle 6$, $\angle 4$ & $\angle 5$

Alternate exterior angles: $\angle 1$ & $\angle 8$, $\angle 2$ & $\angle 7$

Corresponding angles: $\angle 1$ & $\angle 5$, $\angle 2$ & $\angle 6$, $\angle 3$ & $\angle 7$, $\angle 4$ & $\angle 8$

Same-side interior angles: $\angle 3$ & $\angle 5$, $\angle 4$ & $\angle 6$

Same-side Exterior angles: $\angle 1$ & $\angle 7$, $\angle 2$ & $\angle 8$



23. Use the figure to prove the Same-Side Interior Angle Converse Theorem.
 Given: $\angle 7$ and $\angle 6$ are supplementary.
 Prove: $l \parallel m$

$\angle 7 \text{ \& } \angle 6 \text{ supp given}$ $\angle 5 \text{ \& } \angle 6 \text{ L.P.}$
 $m \angle 7 + m \angle 6 = 180$ (def of supp.) $m \angle 5 + m \angle 6 = 180$ (L.P. Postulate)
 $m \angle 7 + m \angle 6 = m \angle 5 + m \angle 6$ (substitution)
 $m \angle 7 = m \angle 5$ (subtraction)
 $\angle 7 \cong \angle 5$ (POCA)
 $l \parallel m$ (Corresponding \angle converse Postulate)

NOTE:
 corresponding angle converse postulate tells us IF corresponding angles are congruent THEN the lines are parallel.
 We proved corresponding \angle 's ($\angle 5 \cong \angle 7$) are congruent so the lines are \parallel .

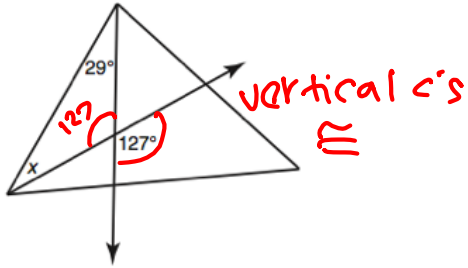
24.

Linear Pair - add to 180

$180 - 95 = 85$
 $85 + 8x + 5 + 5x - 1 = 180$
 $13x + 89 = 180$
 $\quad - 89 \quad - 89$
 $13x = 91$
 $\frac{13x}{13} = \frac{91}{13}$
 $x = 7$

angles of a Δ add to 180.

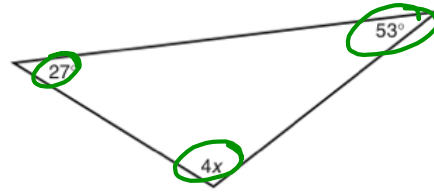
25.



$$\begin{array}{r}
 x + 29 + 127 = 180 \\
 -29 \quad -127 \quad -29 \\
 \hline
 + -127 =
 \end{array}$$

$$x = 24^\circ$$

26.

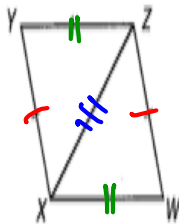


$$\begin{array}{r}
 27 + 53 + 4x = 180 \\
 -27 \quad -53 \\
 \hline
 + + 4x =
 \end{array}$$

$$4x = 100$$

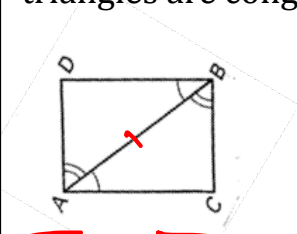
$$x = 25$$

27. Prove that the two triangles are congruent. Use your method of choice.



| Statement | Reason |
|-------------------------------------|-----------|
| $\overline{XY} \cong \overline{WZ}$ | given |
| $\overline{YZ} \cong \overline{XW}$ | given |
| $\overline{XZ} \cong \overline{XZ}$ | reflexive |
| $\triangle XYZ \cong \triangle ZWX$ | SSS |

28. Which postulate or theorem can be used to prove that the triangles are congruent?



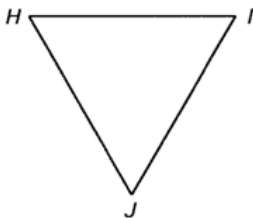
$\overline{AB} \cong \overline{AB}$
reflexive

ASA

29. Fill in the missing parts of the table to complete the two-column proof.

Given: $HI = 8, IJ = 8, \overline{IJ} \cong \overline{JH}$

Prove: $\overline{HI} \cong \overline{JH}$



Statements

1. $HI = 8$
2. $IJ = 8$
3. $HI = IJ$
4. $\overline{HI} \cong \overline{IJ}$
5. $\overline{IJ} \cong \overline{JH}$
6. $\overline{HI} \cong \overline{JH}$

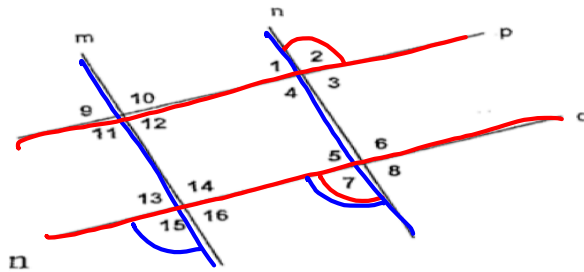
Reasons

1. Given
2. Given
3. Transitive/Substitution
4. DOCS (definition of \cong segments)
5. Given
6. Transitive/Substitution

30. Complete the following proof using the method of your choice.

Given: $m \parallel n$ and $p \parallel q$

Prove: $\angle 2 \cong \angle 15$



$m \parallel n$
given

$p \parallel q$
given

$\angle 7 \cong \angle 15$
Corresponding
 \angle 's

$\angle 2 \cong \angle 7$
AEA

$\angle 2 \cong \angle 15$
transitive
or (Substitution)